Sequences & Series

Precalculus

Arithmetic Sequences

1. Define an <u>arithmetic sequence</u> and given an example.

- 2. For each of the sequences below, determine the <u>common difference</u>, the <u>explicit formula</u>, and the <u>63rd term</u> in the sequence.
 - **a.** 3, 11, 19, 27, ...

b. 26, 21, 16, 11, ...

c. $\frac{3}{4}, \frac{5}{4}, \frac{7}{4}, \frac{9}{4}, \dots$

- 3. For each sequence below, two terms are given. Determine the <u>common difference</u> and <u>explicit formula</u> for each sequence.
 - **a.** $a_{16} = -68, a_{35} = -182$
 - **b.** $a_{10} = 54, a_{33} = 123$

Geometric Sequences

4. Define a geometric sequence and given an example.

5. For each of the sequences below, determine the <u>common ratio</u>, the <u>explicit formula</u>, and the <u>63rd term</u> in the sequence.

a. 1, -3, 9, -27, ...

b. 20, 5, $\frac{5}{4}$, $\frac{5}{8}$, ...

Sigma Notation

6. Find the following sums <u>by hand</u> (there are formulas, but I am simply looking for you to understand what this notation is asking you to find).

$$\sum_{m=7}^{11} 4m - 3$$

 $\sum_{n=1}^{5} \frac{4^n}{3}$

Recursive Formulas

7. If $a_{13} = 11$ and $a_n = a_{n-1} + 5$, find a_{17} . Show all relevant work.

8. If $a_3 = 5$ and $a_n = -3(a_{n-1})$, find a_9 . Show all relevant work.

9. If $a_1 = -2$ and $a_n = n + 3a_{n-1}$, find the sum of the first five terms (S₅).